

Translate Graphs of Polynomial Functions

Compare the function with the graph of $f(x) = x^3$.

1. $g(x) = x^3 + 4$

2. $f(x) = x^3 - 3$

3. $h(x) = (x - 4)^3 + 2$

4. $f(x) = (x + 2)^3 + 1$

Compare the function with the graph of $f(x) = x^4$.

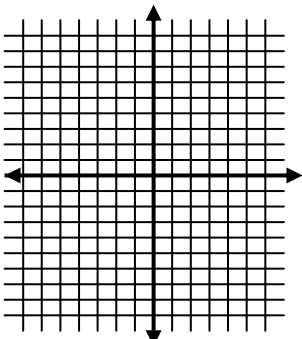
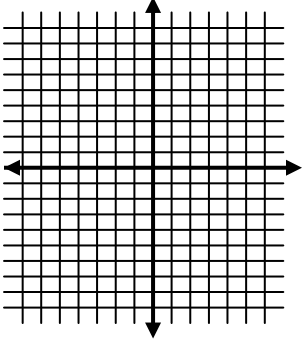
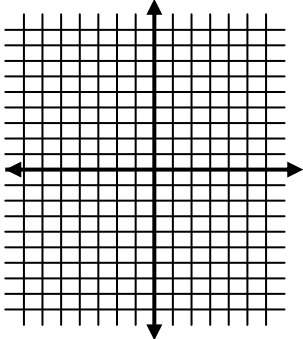
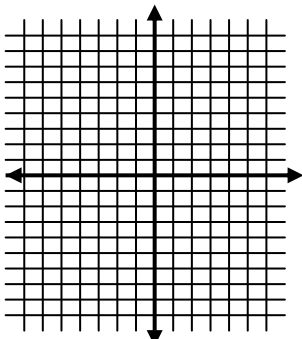
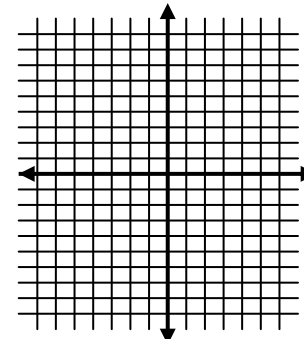
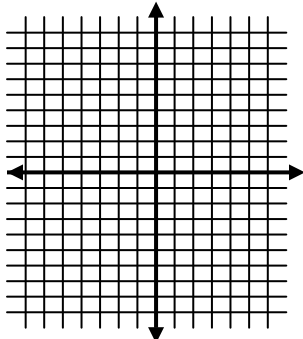
1. $g(x) = x^4 + 3$

2. $f(x) = (x - 1)^4$

3. $h(x) = (x + 5)^4 - 2$

4. $f(x) = (x - 3)^4 - 3$

Do you Remember?...

| <table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 5px;">x</th> <th style="padding: 5px;">f(x)</th> </tr> </thead> <tbody> <tr><td style="padding: 5px;">2</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">1</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">0</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">-1</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">-2</td><td style="padding: 5px;"></td></tr> </tbody> </table> | x | f(x) | 2 | | 1 | | 0 | | -1 | | -2 | | <table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 5px;">x</th> <th style="padding: 5px;">f(x)</th> </tr> </thead> <tbody> <tr><td style="padding: 5px;">2</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">1</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">0</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">-1</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">-2</td><td style="padding: 5px;"></td></tr> </tbody> </table> | x | f(x) | 2 | | 1 | | 0 | | -1 | | -2 | | <table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 5px;">x</th> <th style="padding: 5px;">f(x)</th> </tr> </thead> <tbody> <tr><td style="padding: 5px;">2</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">1</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">0</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">-1</td><td style="padding: 5px;"></td></tr> <tr><td style="padding: 5px;">-2</td><td style="padding: 5px;"></td></tr> </tbody> </table> | x | f(x) | 2 | | 1 | | 0 | | -1 | | -2 | |
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| -2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Linear | Absolute Value | Quadratic | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| Domain: | Domain: | Domain: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Range: | Range: | Range: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| -2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| x | f(x) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| Cubic | Square Root | Rational | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Equation: | Equation: | Equation: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| Domain: | Domain: | Domain: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Range: | Range: | Range: | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Math Instructional Framework

| | |
|---------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Full Name | |
| Time Frame | 6 weeks - Unit 5 |
| Unit Name | Polynomials |
| Learning Task/Topics/ Themes | Simple Polynomial Translations of $f(x) = ax^n$ |
| Standards and Elements | MM3A1 – Students will analyze graphs of polynomial functions of higher degree. a. Graph simple polynomial functions as translations of the function $f(x) = ax^n$. |
| Lesson Essential Questions | How do you graph simple translations of the function $f(x) = ax^n$? |
| Activator | Use the graphic organizer, Basic Functions, to review the parent graphs from Math 1 and 2. |
| Vocabulary | Translation, Polynomial Function, Cubic, Quartic, Quintic |
| Work Session | Guided Practice – Polynomial Functions Translations Graphic Organizer Over Cubics, Quartics, and Quintics Student Independent Practice – Translate Polynomial Functions Worksheet |
| Summarizing/Closing/Formative Assessment | Think-Pair-Share Students create a translation of a graph written in function notation. Have students switch papers. Students tell the translation for one another's problem. |

Polynomial Function

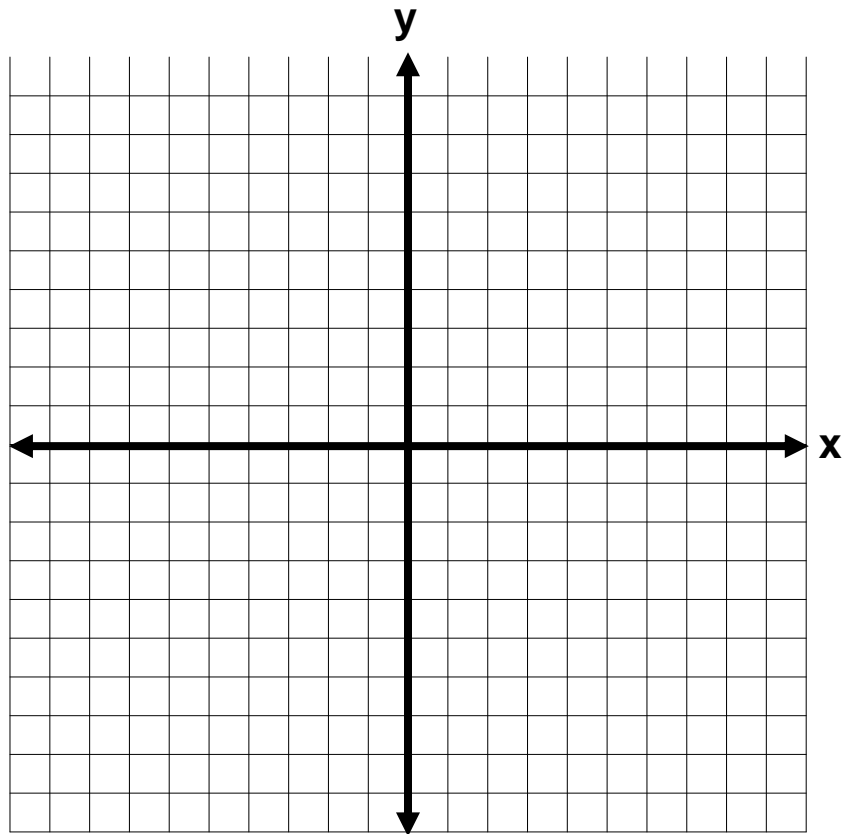
$$f(x) = x^3$$

Plot the points and sketch the graph below.

Complete the table of values.

| x | f(x) |
|----|------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |

Why is this called a cubic function?



What is the x-intercept?

What is the y-intercept?

What is the domain?

What is the range?

How could this graph be shifted up or down?

Families Of Cubic Functions in the Form of $f(x) = x^3 + p$

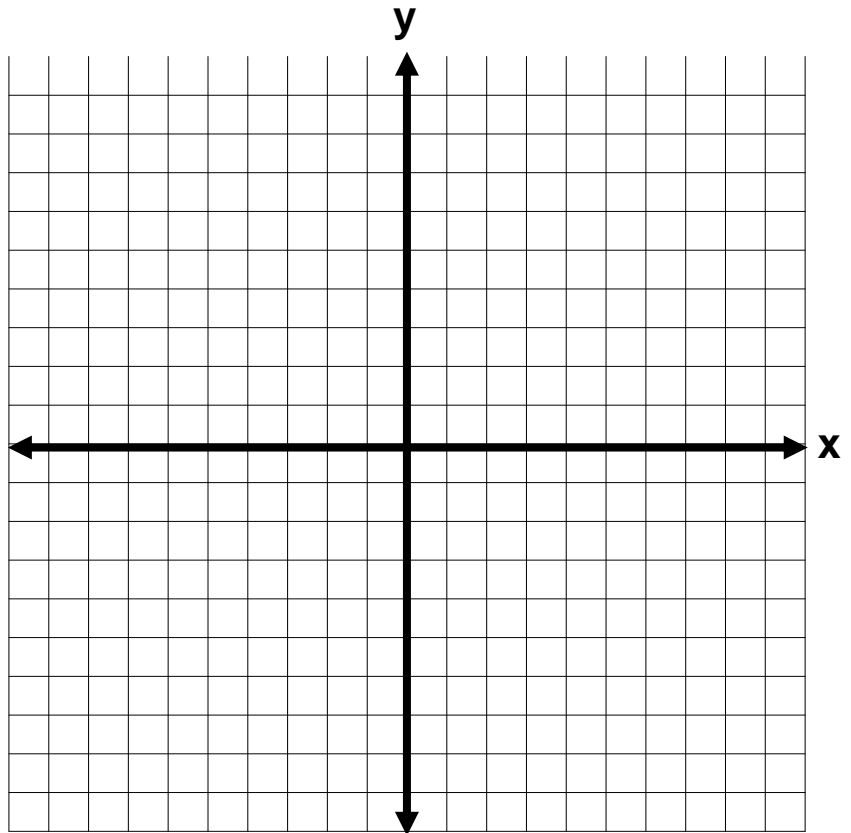
Graph each of the following functions in different colors on the graph at the right.

$$f(x) = x^3 + 4$$

$$f(x) = x^3 - 5$$

$$f(x) = (x - 2)^3$$

$$f(x) = (x + 3)^3$$



How are the graphs alike?

How are the graphs different?

How would the graph of $f(x) = x^3 - 3$ compare to the graph of $f(x) = x^3$?

How would the graph of $f(x) = x^3 + 4$ compare to the graph of $f(x) = x^3$?

How would the graph of $f(x) = (x - 2)^3$ compare to the graph of $f(x) = x^3$?

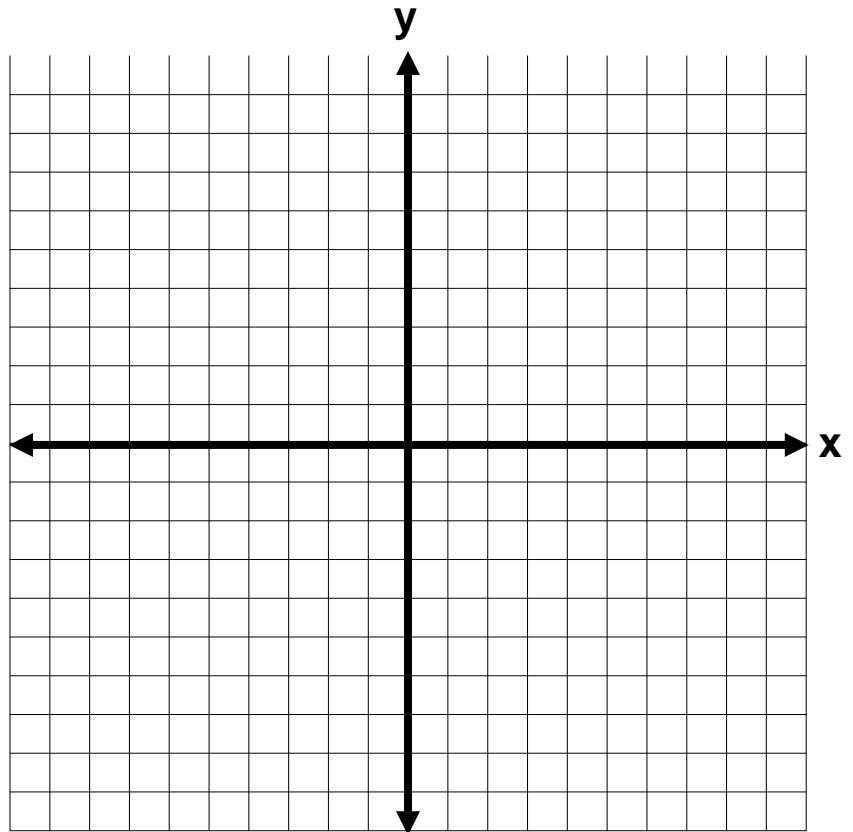
Polynomial Function

$$f(x) = x^4$$

Plot the points and sketch the graph below.

Complete the table of values.

| x | f(x) |
|----|------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |



Why is this called a quartic function?

What is the x-intercept?

What is the y-intercept?

What is the domain?

What is the range?

How could this graph be shifted up or down?

**Families
Of Quartic
Functions in
the Form of
 $f(x) = x^4 + n$**

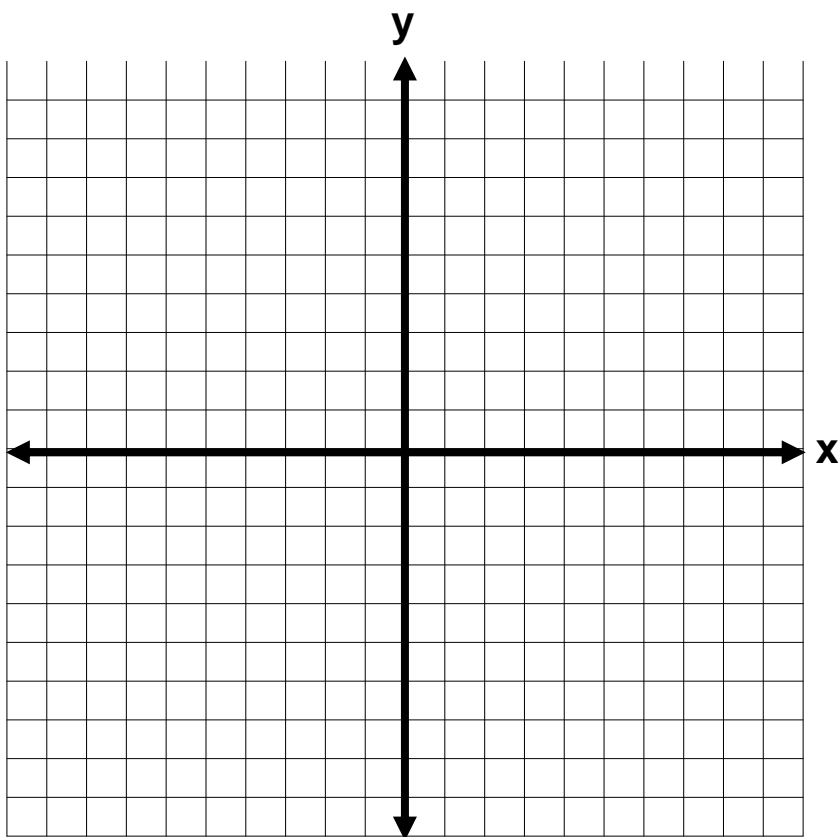
Graph each of the following functions in different colors on the graph at the right.

$$f(x) = x^4 + 3$$

$$f(x) = x^4 - 2$$

$$f(x) = (x - 1)^4$$

$$f(x) = (x + 2)^4$$



How are the graphs alike?

How are the graphs different?

How would the graph of $f(x) = x^4 - 2$ compare to the graph of $f(x) = x^4$

How would the graph of $f(x) = x^4 + 3$ compare to the graph of $f(x) = x^4$

How would the graph of $f(x) = (x - 5)^4$ compare to the graph of $f(x) = x^4$

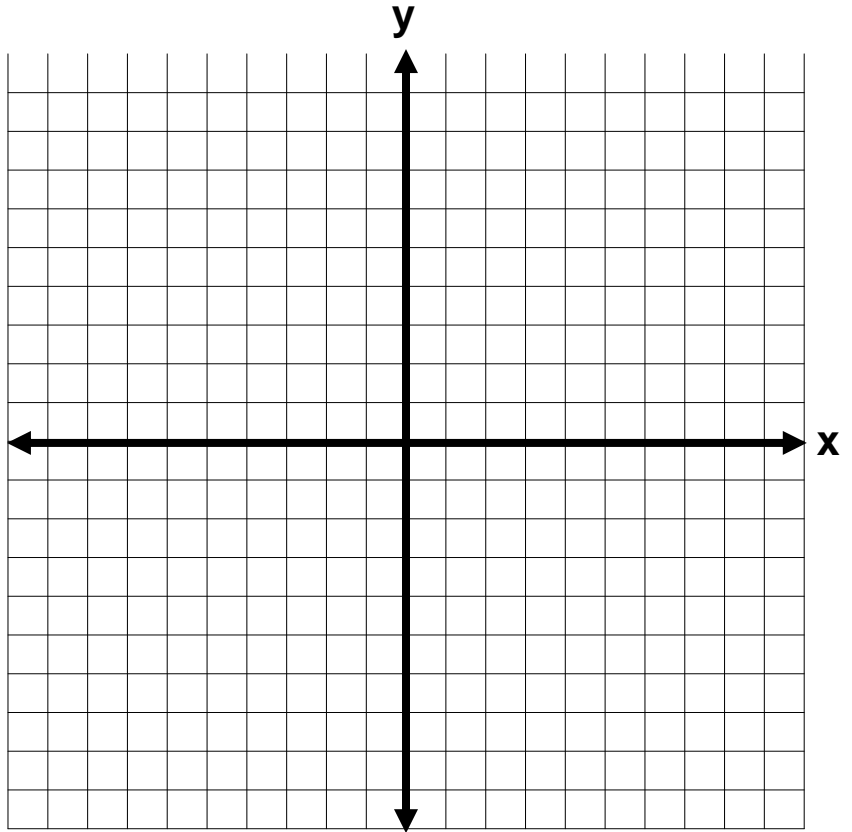
Polynomial Function

$$f(x) = x^5$$

Plot the points and sketch the graph below.

Complete the table of values.

| x | f(x) |
|----|------|
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |



Why is this called a quintic function?

What is the x-intercept?

What is the y-intercept?

What is the domain?

What is the range?

How could this graph be shifted up or down?

**Families
Of Quintic
Functions in
the Form of
 $f(x) = x^5 + n$**

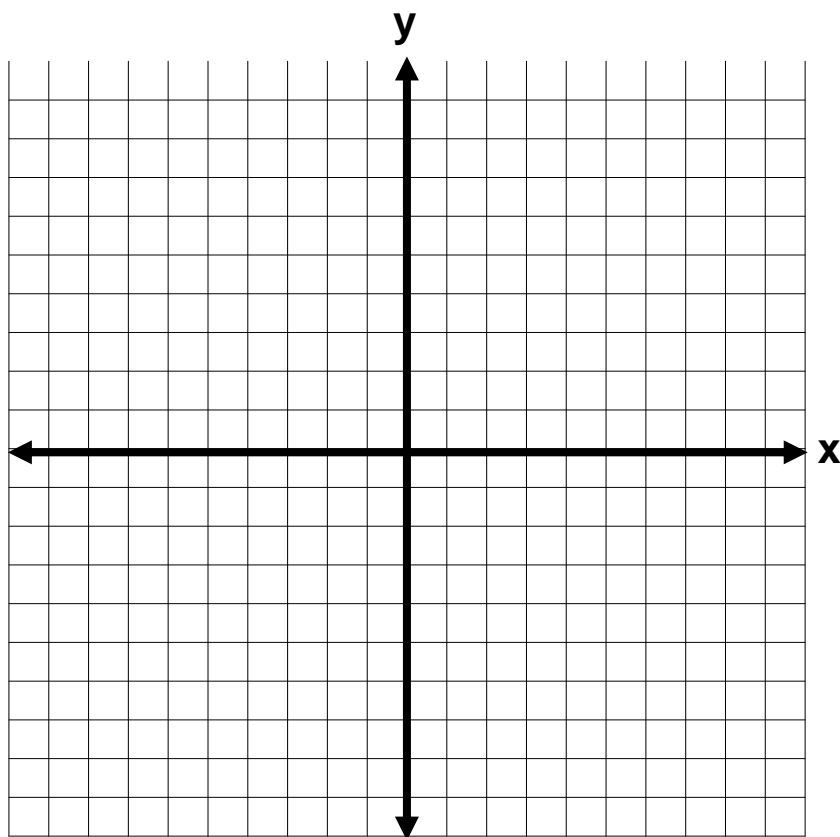
Graph each of the following functions in different colors on the graph at the right.

$$f(x) = x^5 - 3$$

$$f(x) = x^5 + 2$$

$$f(x) = (x + 4)^5$$

$$f(x) = (x - 5)^5$$



How are the graphs alike?

How are the graphs different?

How would the graph of $f(x) = x^5 - 4$ compare to the graph of $f(x) = x^5$?

How would the graph of $f(x) = x^5 + 2$ compare to the graph of $f(x) = x^5$?

How would the graph of $f(x) = (x + 1)^5$ compare to the graph of $f(x) = x^5$?