

Acquisition Lesson Planning Form
Plan for the Concept, Topic, or Skill – Equations of Circles
Key Standards addressed in this Lesson: MM3G1a,b
Time allotted for this Lesson:

Standard: MM3G1a,b: Find the equations of circles. Graph a circle given an equation in general form.
Essential Question: How do I identify the characteristics of circles from equations? What characteristics of circles are necessary to graph and write the equations of circles?
Activating Strategies: Worksheet Prerequisite Skills for Unit 2 Use K – W – L to determine what the students already know about circles, their equations, and how to graph.
Acceleration/Previewing: (Key Vocabulary) Circle, radius, center, general form, standard form
Teaching Strategies: Use the graphic organizer to demonstrate how to graph and write the equation of circle. Circle Learning Task Part I
Task: Circle Learning Task
Distributed Guided Practice: Worksheet Lesson 1: Equations of Circles
Extending/Refining Strategies: Journal: Have students explain how to graph a circle given the center and the radius.
Summarizing Strategies: Ticket Out the Door

PreRequisite Skills for Unit 2

Midpoint Formula $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

1. (7,4),(9,-1) 2. (8,-9),(0,5) 3. (1,-7),(-1,-12)

Distance Formula $d = \sqrt{x_2 - x_1)^2 + (y_2 - y_1)^2}$

4. (2,0),(10,6) 5. (7,4),(9,-1) 6. (2,-3),(-4,-13)

Completing the square

$ax^2 + bx + c = 0$

$ax^2 + bx + c = 0$

1. a must be 1 (factor out if necessary)

2. rewrite equation leaving a blank and moving c to other side

$x^2 + bx + \underline{\hspace{1cm}} = -c + \underline{\hspace{1cm}}$

3. take half the linear term (b) and square that number

4. add that number to both sides of the equation

$x^2 + bx + (\frac{1}{2}b)^2 = -c + (\frac{1}{2}b)^2$

5. rewrite as $(a \pm \frac{1}{2}b)^2 =$ add right side

$(x + \frac{1}{2}b)^2 = \underline{\hspace{1cm}}$

7. $x^2 + 10x - 21 = 0$

$x^2 + 10x + \underline{\hspace{1cm}} = 21 + \underline{\hspace{1cm}}$
 $(x + \underline{\hspace{1cm}})^2 = \underline{\hspace{1cm}}$

8. $x^2 - 4x - 12 = 0$

$x^2 - 4x + \underline{\hspace{1cm}} = 12 + \underline{\hspace{1cm}}$
 $(x - \underline{\hspace{1cm}})^2 = \underline{\hspace{1cm}}$

9. $x^2 - 18x + 57 = 60$

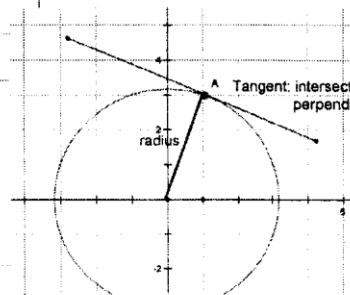
$x^2 - 18x + \underline{\hspace{1cm}} = 3 + \underline{\hspace{1cm}}$
 $(x - \underline{\hspace{1cm}})^2 = \underline{\hspace{1cm}}$

10. $x^2 - 20x - 6 = 7$

(where did the 3 come from?)

11. $x^2 + 5x - 3 = 0$

12. $4x^2 + 24x - 19 = 1$



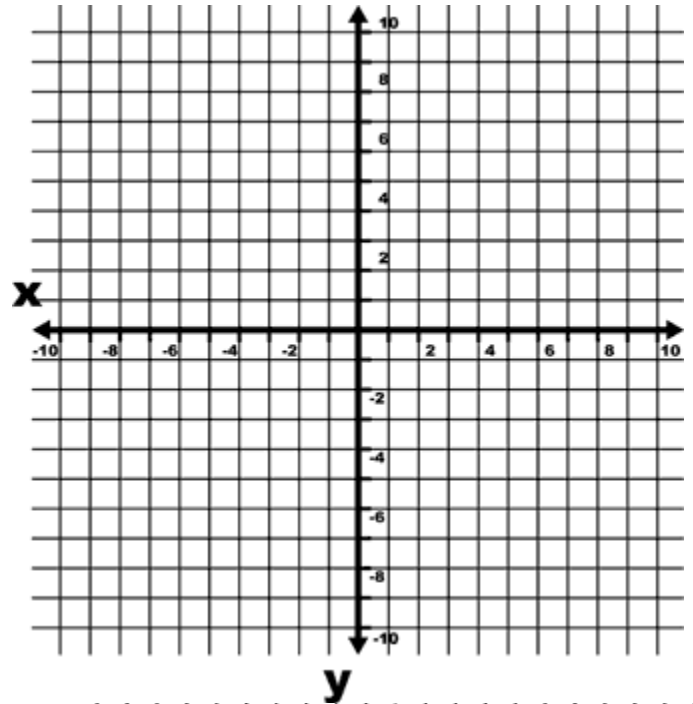
Tangent: intersects a circle at one point perpendicular to the radius

Find the radius if the tangent of the circle is at (1, 3).

Graphic Organizer Writing equations and Graphing circles

To graph a circle from an equation:

- 1.) Write the equation in standard form
 $x^2 + y^2 = r^2$ or $(x - h)^2 + (y - k)^2 = r^2$
 EXAMPLE: $(x - 2)^2 + (y - 1)^2 = 16$
- 2.) Determine the center (h,k), graph center (2,1)
- 3.) Determine the radius
 radius $\sqrt{16} = 4$
- 4.) Graph four points on the circle
 $(2 \pm 4, 1)$ $(2, 1 \pm 4)$
 $(6,1)$ $(-2,1)$ $(2,5)$ $(2,-3)$
- 5.) Connect coordinate points.

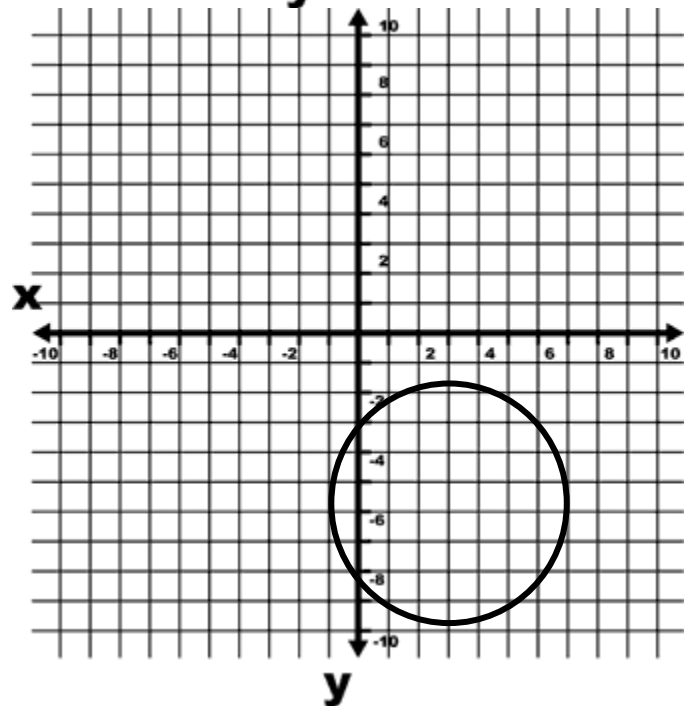


To write an equation for a circle from a graph:

- 1.) Determine the center of the circle (h,k)

- 2.) Determine the radius
 distance between (h,k) and a point on the circle (x,y)
 $d = \sqrt{(x - h)^2 + (y - k)^2}$

- 3.) Write in standard form of equation of a circle.
 $x^2 + y^2 = r^2$ or $(x - h)^2 + (y - k)^2 = r^2$

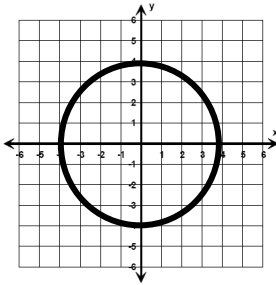


Guided Practice
Lesson 1: Equations of Circles

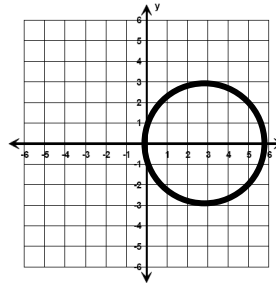
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Write the standard equation for each circle graphed below:

1.



2.



Write the standard equation of a circle with each given radius and center:

3. $r = 4$; $C(0,0)$

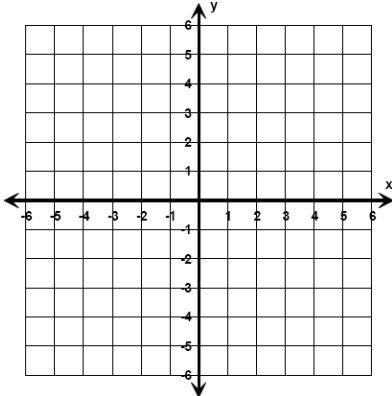
4. $r = 1$; $C(2,3)$

5. $r = 10$; $C(-2,-7)$

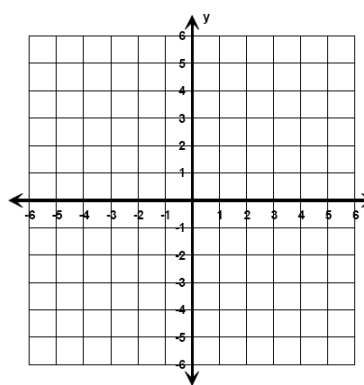
6. $r = 1/3$; $C(-2,-2)$

Graph each equation. Label the center and the radius.

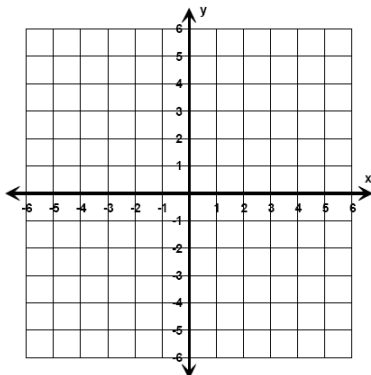
7. $x^2 + y^2 = 9$



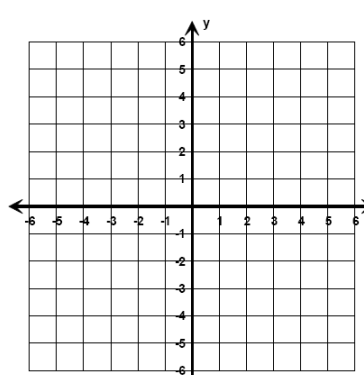
8. $(x - 2)^2 + y^2 = 4$



9. $(x + 3)^2 + (y + 1)^2 = 4$



10. $(x)^2 + (y + 3)^2 = 25$



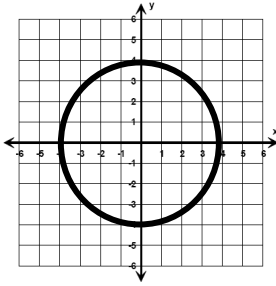
Guided Practice
Lesson 1: Equations of Circles

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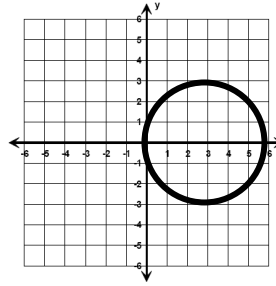
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Write the standard equation for each circle graphed below:

1.



2.



Write the standard equation of a circle with each given radius and center:

3. $r = 4$; $C(0,0)$

$x^2 + y^2 = 16$

4. $r = 1$; $C(2,3)$

$(x - 2)^2 + (y - 3)^2 = 1$

5. $r = 10$; $C(-2,-7)$

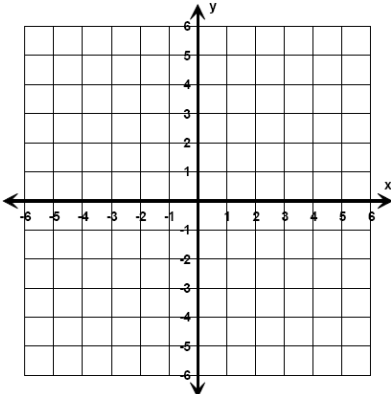
$(x + 2)^2 + (y + 7)^2 = 100$

6. $r = 1/3$; $C(-2,-2)$

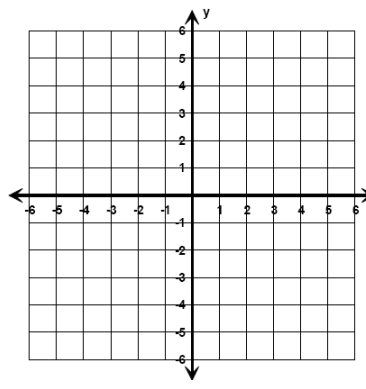
$(x + 2)^2 + (y + 2)^2 = 1/9$

Graph each equation. Label the center and the radius.

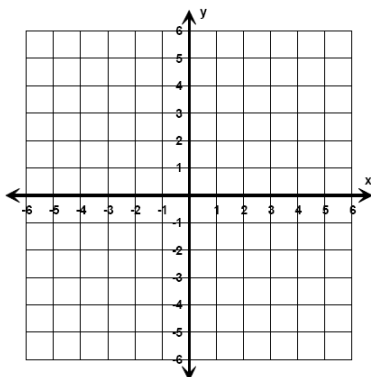
7. $x^2 + y^2 = 9$



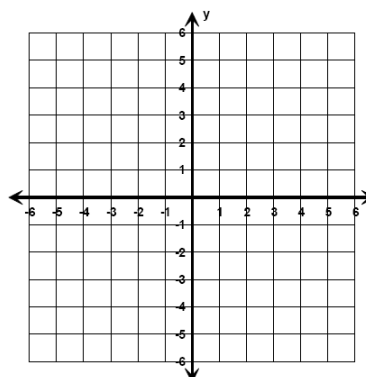
8. $(x - 2)^2 + y^2 = 4$



9. $(x + 3)^2 + (y + 1)^2 = 4$

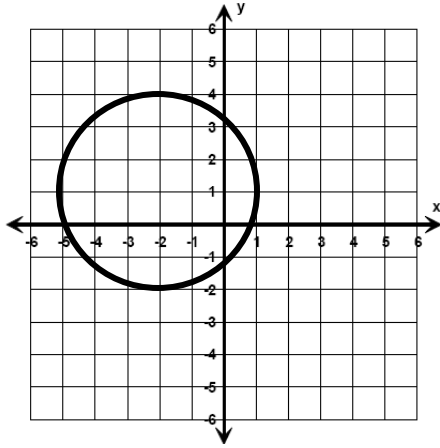


10. $(x)^2 + (y + 3)^2 = 25$



Write the standard equation for the circle graphed below:

1.



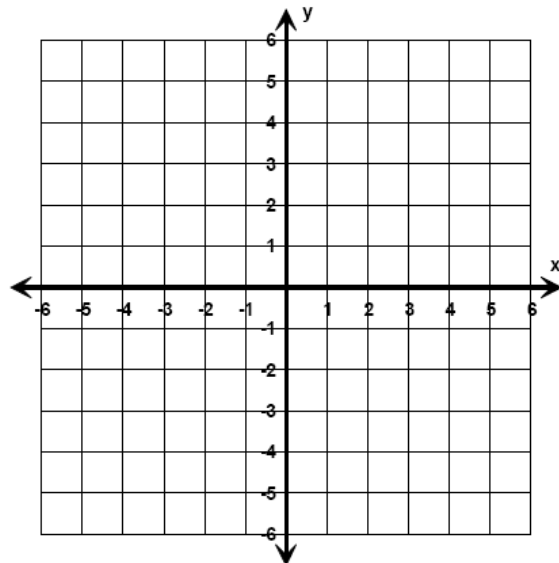
Write the standard equation of a circle with each given radius and center:

2. $r = \frac{1}{4}$; $C(1,0)$

3. $r = 15$; $C(-6,9)$

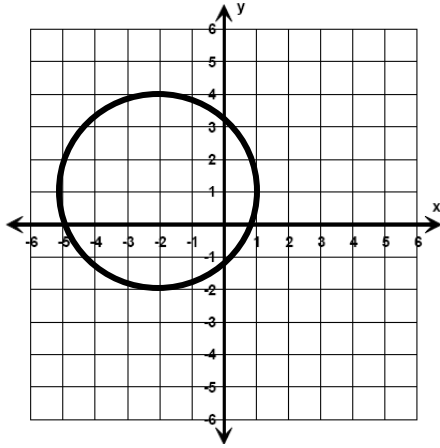
Graph the following equation. Label the center and radius.

4. $(x + 2)^2 + (y - 4)^2 = 16$



Write the standard equation for the circle graphed below:

1.



Write the standard equation of a circle with each given radius and center:

2. $r = \frac{1}{4}$; $C(1,0)$

3. $r = 15$; $C(-6,9)$

$$(x - 1)^2 + (y)^2 = 1 / 16$$

$$(x + 6)^2 + (y - 9)^2 = 225$$

Graph the following equation. Label the center and radius.

4. $(x + 2)^2 + (y - 4)^2 = 16$

